

- 1) X , λ parametresi ile üstel dağılıma uygun bir rassal değişken ise,
- a) $P(X = t) = f(t) = \lambda e^{-\lambda t}$
- b) $P(X > t) = 1 - F(t) = e^{-\lambda t}$
- c) $E[X] = \frac{1}{\lambda}$
- 2) Üstel dağılımın unutkanlık özelliği vardır. Buna göre,
 $P(X > t + s | X > t) = P(X > s)$,
- 3) T , λ parametresi ile poisson dağılıma uygun bir rassal değişken ise, t döneminde n olay olma olasılığı
 $p_n(t) = \frac{(\lambda t)^n e^{-\lambda t}}{n!}$
- 4) Kuyruk uzunluğu N ve hizmet sıklığı μ olan, saf ölüm modeline uygun bir kuyruk sisteminde, t anında, n müşteri kalma olasılığı, $p_n(t) = \frac{(\mu t)^{N-n} e^{-\mu t}}{(N-n)!}$ dir.
- 5) Genelleştirilmiş Poisson Kuyruk Modelinde;

- a) Sistemde n müşteri olma olasılığı;

$$p_n = \left(\frac{\lambda_{n-1} \lambda_{n-2} \cdots \lambda_1 \lambda_0}{\mu_n \mu_{n-1} \cdots \mu_2 \mu_1} \right) p_0$$

- b) Sistemde hiç müşteri olmama olasılığı;

$$p_0 = 1 - \sum_{n=1}^{\infty} p_n$$

- 6) Kararlılık durumu performans ölçütleri;

- a) $L_s = \sum_{n=1}^{\infty} n p_n = \lambda_{eff} W_s$
- b) $L_q = \sum_{n=(c+1)}^{\infty} (n - c) p_n = \lambda_{eff} W_q$
- c) $W_s = W_q + \frac{1}{\mu}$
- d) $L_s = L_q + \frac{\lambda_{eff}}{\mu}$
- e) $\bar{c} = L_s - L_q = \frac{\lambda_{eff}}{\mu}$
- f) $\rho = \frac{\lambda}{\mu}$
- g) $\lambda = \lambda_{eff} + \lambda_{lost}$

- 7) (M/M/1):(GD/∞/∞) ;

- a) $p_n = \left(\frac{\lambda}{\mu} \right)^n p_0 = \rho^n p_0$
- b) $p_0 = 1 - \rho$
- c) $L_s = \frac{\rho}{1 - \rho}$
- d) $W_s = \frac{L_s}{\lambda} = \frac{1}{\mu(1 - \rho)}$
- e) $W_q = W_s - \frac{1}{\mu} = \frac{\rho}{\mu(1 - \rho)}$
- f) $L_q = \lambda W_q = \frac{\rho^2}{(1 - \rho)}$
- g) $\bar{c} = L_s - L_q = \rho$

- 8) (M/M/1):(GD/N/∞) ;

- a) $p_n = \begin{cases} \rho^n p_0 & n \leq N \\ 0 & n > N \end{cases}$
- b) $p_0 = \begin{cases} \frac{(1 - \rho) \rho^n}{1 - \rho^{N+1}} & \rho \neq 1 \\ \frac{1}{N+1} & \rho = 1 \end{cases}$
- c) $\lambda_{lost} = \lambda p_N$
- d) $\lambda_{eff} = \lambda(1 - p_N)$
- e) $L_s = \begin{cases} \sum_{n=0}^N n p_n = \frac{\rho \{1 - (N+1) \rho^N + N \rho^{N+1}\}}{1 - \rho} & \rho \neq 1 \\ \frac{N}{2} & \rho = 1 \end{cases}$
- f) $W_s = \frac{L_s}{\lambda_{eff}}$
- g) $W_q = W_s - \frac{1}{\mu}$
- h) $L_q = \lambda_{eff} W_q$
- i) $\bar{c} = L_s - L_q = \rho$

- 9) (M/M/c):(GD/∞/∞) ;

- a) $p_n = \begin{cases} \frac{\lambda^n}{n! \mu^n} p_0 & n \leq c \\ \frac{\lambda^n}{c! c^{n-c} \mu^n} p_0 & n > c \end{cases}$
- b) $p_0 = \left\{ \sum_{n=0}^{c-1} \frac{\rho^n}{n!} + \frac{\rho^c}{c!} \left(\frac{1}{1 - \frac{\rho}{c}} \right) \right\}^{-1} \quad \frac{\rho}{c} < 1$
- c) $L_q = \sum_{n=c}^{\infty} (n - c) p_n = \frac{\rho^{c+1}}{(c-1)!(c-\rho)^2} p_0$
- d) $L_s = L_q + \rho$
- e) $\lambda_{eff} = \lambda, \quad W_s = \frac{L_s}{\lambda}, \quad W_q = \frac{L_q}{\lambda}$

- 10) (M/M/c):(GD/N/∞) ; $c \leq N$

- a) $p_n = \begin{cases} \frac{\rho^n}{n!} p_0 & 0 \leq n \leq c \\ \frac{\rho^n}{c! c^{n-c}} p_0 & c < n \leq N \end{cases}$
- b) $p_0 = \begin{cases} \left[\sum_{n=0}^{c-1} \frac{\rho^n}{n!} + \frac{\rho^c \left(1 - \left(\frac{\rho}{c} \right)^{N-c+1} \right)}{c! \left(1 - \frac{\rho}{c} \right)} \right]^{-1} & \frac{\rho}{c} \neq 1 \\ \left[\sum_{n=0}^{c-1} \frac{\rho^n}{n!} + \frac{\rho^c}{c!} (N - c + 1) \right]^{-1} & \frac{\rho}{c} = 1 \end{cases}$
- c) $L_q = \frac{\rho^{c+1}}{(c-1)!(c-\rho)^2} \left\{ 1 - \left(\frac{\rho}{c} \right)^{N-c+1} - (N - c + 1) \left(1 - \frac{\rho}{c} \right) \left(\frac{\rho}{c} \right)^{N-c} \right\} p_0$
- d) $\frac{\rho}{c} = 1$ için $L_q = \frac{\rho^c (N - c) (N - c + 1)}{2c!} p_0$
- e) $\lambda_{lost} = \lambda p_N$
- f) $\lambda_{eff} = \lambda - \lambda_{lost}, \quad W_s = \frac{L_s}{\lambda_{eff}}, \quad W_q = \frac{L_q}{\lambda_{eff}}$

- 11) (M/M/∞):(GD/∞/∞) – Self Servis Modeli

- a) $p_n = \frac{e^{-\rho} \rho^n}{n!} \quad n = 0, 1, 2, \dots$
- b) $L_s = \rho, \quad L_q = W_q = 0$